



THE CHINESE UNIVERSITY OF HONG KONG
 Institute of Network Coding
 and
 Department of Information Engineering
Seminar



Vector versus Scalar Linear Codes for Multicast Network Coding

by

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Abstract

Vector linear network coding (LNC) is a generalization of the conventional scalar LNC, such that the data unit transmitted on every edge is an L -dimensional vector of data symbols over a base field $\text{GF}(q)$. There are classical exemplifying multi-source networks that have simple vector linear solutions but do not have a scalar linear solution over any field.

For (single-source) multicast networks, it has been conjectured and partially proved by Ebrahimi and Fragouli that vector LNC has the following benefits over scalar LNC in terms of alphabet size of data units:

- i) A multicast network scalar linearly solvable over $\text{GF}(q^{L_1})$ and $\text{GF}(q^{L_2})$ may not be scalar linearly solvable over $\text{GF}(q^{L_1+L_2})$, but a multicast network vector linearly solvable of dimensions L_1 and L_2 over $\text{GF}(q)$ must be vector linearly solvable of dimension $L_1 + L_2$ over $\text{GF}(q)$;
- ii) There exists a multicast network that is vector linearly solvable of dimension L over $\text{GF}(q)$ but not scalar linearly solvable over any field of size $q' \leq q^L$.

In this talk, we affirm the above two conjectures to be correct by explicit exemplifying networks, which are constructed by a general method to be introduced. Moreover, among these exemplifying networks vector linearly solvable of dimension L over $\text{GF}(q)$, there are instances with the additional property that even for some $q' > q^L$, they are still not scalar linearly solvable over $\text{GF}(q')$.

On the other hand, we also demonstrate a few multicast networks where scalar LNC outperforms vector LNC in the sense that they do not have a vector linear solution of dimension L over $\text{GF}(2)$ but have a scalar linear solution over $\text{GF}(q')$ for some $q' < 2^L$.

Biography

Qifu (Tyler) Sun received the B.Eng. (first class honors) and Ph.D. degrees from the Department of Information Engineering, The Chinese University of Hong Kong in 2005 and 2009, respectively. He has been a postdoctoral fellow at the Institute of Network Coding, The Chinese University of Hong Kong and a visiting fellow at the University of New South Wales. He is currently an associate professor at the School of Computer & Communication Engineering, University of Science and Technology Beijing. His research interests include fundamental study of network coding, channel coding and modulation, and algebraic study of communication networks. He is currently the principal investigator of two grants of National Natural Science Foundation of China.

**** ALL ARE WELCOME ****